

# College of AI – Preliminary Exam Syllabus

## Rules

- (1) **You have 3 hours.**
  - (2) **Total: 100 points.** In order to pass, PhD students should get at least **60** points.
  - (3) **Closed-book.** You may bring **five A4 pages** (hand-written or printed on both sides). **No** books, computers, or cellphones.
  - (4) You have to prepare for **one subarea**. There will be problems for each subarea in the exam. You only need to answer the problem in the subarea you choose.
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## General Requirements (85%)

### 1. Basic Algorithms

#### (1) **Sorting**

Bubble sort, insertion sort, merge sort, heapsort, quicksort

#### (2) **Basic Data Structures**

Binary search tree (CLRS Ch.12)

#### (3) **Basic Graph Problems**

- a. BFS, DFS
- b. Connected components
- c. Directed acyclic graphs and topological order (CLRS 22.4, 22.5)

#### (4) **Minimum Spanning Tree**

- a. Prim algorithm (KT 4.5, 4.6)
- b. Can use MST to model and solve other problems

#### (5) **Dynamic Programming** (KT Ch.6, CLRS Ch.15) – can use DP to solve problems

#### (6) **Greedy Algorithms** (KT Ch.4, CLRS Ch.16)

- a. Interval scheduling (KT 4.1)
- b. Scheduling to minimize lateness (KT 4.2)
- c. Huffman codes (KT 4.8)

(7) **Basic Linear Programming** (CLRS Ch.29) – know what a linear program is

## 2. Solving Problem by Search (AI Book Chapter 3), Beyond classic search (AI Book Chapter 4)

## 3. Basic Machine Learning

(1) <https://www.coursera.org/learn/machine-learning>

(2) Things you need to know: Bias-Variance trade-off, overfitting,  $k$ -means,  $k$ -nn, PCA, Random Forest, AdaBoost, Gradient Boosting, Expectation Maximization (EM), (Stochastic) Gradient Descent, SVM, kernel, lasso

## 4. Deep Learning

(1) <https://cs231n.stanford.edu/2024/> (Lecture 1-13)

(2) **Deep Neural Network Architectures:** multi-layer perceptron, Autoencoders, Convolutional neural network, Transformers

(3) **Basic Components of Deep Learning** [see [DL book] Ch.7-15]: Backpropagation, Activation functions, Regularization for Deep Learning, Optimization Algorithms for Training Deep Model

(4) **Sequence Modelling:** Recurrent nets, Seq2seq model, Attention

(5) **Generative Models:** basic concepts of generative models; basic definition and idea of energy-based model, flow model, VAE, GAN, diffusion models

(6) **Science of Deep Learning (why does deep learning work):** benefits of depth, properties of loss landscape (e.g., mode connectivity), training dynamics (e.g., grokking) [UDL book Ch.20]

## 5. Basic Reinforcement Learning

## 6. Basic Mathematics

Everything you learn from the calculus, linear algebra, and probability course, convex optimization [CO book].

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## Reference

[DL book] **Deep Learning.** Ian Goodfellow, Yoshua Bengio & Aaron Courville.

<https://www.deeplearningbook.org/>

[AI Book] **Artificial Intelligence: A Modern Approach.** 3rd Ed. Stuart Russell & Peter Norvig

[RL book] **Reinforcement Learning: An Introduction** (2nd Ed.). Richard Sutton & Andrew Barto

[CV book] **Foundations of Computer Vision** – Antonio Torralba, Phillip Isola & William T. Freeman, MIT Press (2024)

[Math book] **Mathematics for Machine Learning**. A. Aldo Faisal, Cheng Soon Ong, Marc Peter Deisenroth

[ML book] **Pattern Recognition and Machine Learning**. Christopher Bishop.

<https://www.microsoft.com/en-us/research/wp-content/uploads/2006/01/Bishop-Pattern-Recognition-and-Machine-Learning-2006.pdf>

[DL Course] **Stanford CS336 Language Modeling from Scratch**.

[UDL book] **Understanding Deep Learning**. Simons J.D. Prince.

[CO book] **Convex Optimization**. Stephen Boyd & Lieven Vandenberghe.

<https://web.stanford.edu/~boyd/cvxbook/>

[KT book] **Algorithm Design**. Jon Kleinberg & Eva Tardos.

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## Sub-areas (choose one, 15%)

### Sub-area #1: AI Theory

#### 1. Applied Math

- a. Spectral decomposition
- b. Eigenvalue decomposition
- c. Singular value decomposition
- d. Stochastic process and mixing
- e. Markov Chain Monte Carlo

#### 2. Machine Learning

- a. PAC learning
- b. Bias-Variance tradeoff
- c. VC dimension
- d. SVM
- e. Decision Trees

### Reference Books

[1] Blum, Avrim, John Hopcroft & Ravindran Kannan. *Foundations of Data Science*.

[2] Shalev-Shwartz, Shai & Shai Ben-David. *Understanding Machine Learning: From Theory to Algorithms*. Cambridge UP, 2014.

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# Sub-area #2: Computer Vision

## 1. CV / Overview of Computer Vision

- a. Image Sensing & Acquisition – CCD/CMOS sensors, optics and lens distortions, exposure control, noise models
- b. Camera Geometry & Calibration – pinhole model, intrinsic/extrinsic parameters, epipolar geometry, calibration workflows
- c. Core Vision Task Landscape – low-level (denoising, super-resolution), mid-level (feature extraction, segmentation), high-level (classification, detection, scene understanding)
- d. Benchmark Datasets & Metrics – MNIST, CIFAR, ImageNet, COCO, Cityscapes; evaluation metrics such as accuracy, IoU, mAP, F1

[1] *Computer Vision: Algorithms and Applications, 2 ed.* – Richard Szeliski, Springer (2022)

[2] *Computer Vision Metrics: Survey, Taxonomy, and Analysis of Computer Vision, Visual Neuroscience, and Visual AI, 2 ed.* – Scott Krig, Springer (2025)

## 2. CV / Traditional Techniques

- a. Traditional Filtering & Feature Extraction – Gaussian/median filters, Canny/Harris edges, SIFT & ORB descriptors
- b. Classical Recognition, Tracking & Scene Parsing – Bag-of-Visual-Words, HOG-SVM, Kalman/particle tracking
- c. Geometric & Motion Vision – optical flow, visual odometry

[3] *Feature Extraction and Image Processing for Computer Vision, 4 ed.* – Mark S. Nixon & Alberto S. Aguado, Academic Press (2019)

[4] *Computer Vision: A Modern Approach, 2 ed.* – David A. Forsyth & Jean Ponce, Pearson (2011)

## 3. CV / Deep-Learning Approaches

- a. CNN Architectures & Transfer Learning – modern convolutional backbones, feature reuse, fine-tuning across domains
- b. Detection, Segmentation & Dense Prediction – end-to-end object localization, pixel-wise labeling, panoptic vision tasks
- c. Vision Transformers & Spatiotemporal Models – attention-based encoders, hybrid CNN-Transformer designs, unified spatial-temporal reasoning
- d. Video Understanding & Temporal Modeling – integrated spatial-temporal feature extraction, multi-frame context, sequence-level recognition

[5] *Deep Learning* – Ian Goodfellow, Yoshua Bengio & Aaron Courville, MIT Press (2016)

[6] *Transformers for Natural Language Processing and Computer Vision, 3 ed.* – Denis Rothman, Packt (2024)

#### 4. CV / Self-supervised & Unsupervised Learning

- a. Contrastive Representation Learning – instance-level similarity objectives, multi-view feature alignment
- b. Masked & Predictive Image Modeling – context-driven reconstruction, masked region prediction, spatial forecasting
- c. Generative & Reconstruction-based Learning – latent variable modeling, image generation, and restoration signals
- d. Clustering, Pseudo-Labeling & Domain Adaptation – self-labeling cycles, category discovery, domain-shift adaptation

[7] *A Cookbook of Self-Supervised Learning* – Randall Balestriero et al., arXiv (2023)

[8] *Self-Supervised Learning Crash Course: Unsupervised AI for NLP, Vision, and Beyond* – Packt (2024)

#### 5. CV / Large Models & Multi-Modality

- a. Vision–Language Foundation Models – large-scale joint pre-training on image–text pairs, unified embedding spaces, broad zero-/few-shot transfer across tasks
- b. Multimodal Generation – text-to-image and image-to-text synthesis, coherent cross-modal storytelling, iterative refinement workflows
- c. Modality Alignment – shared representations for retrieval, cross-modal matching and grounding, seamless information flow between visual, linguistic, and other sensor streams

[9] *Multimodal Deep Learning* – Cem Akkus et al., arXiv (2023)

#### 6. CV / 3-D Vision & Simulation

- a. Depth & Geometry Estimation – stereo / monocular depth, multi-view reconstruction, surface fusion
- b. SLAM & Spatial Mapping – visual-inertial localization, loop closure, dense & sparse mapping
- c. Neural Rendering – neural radiance fields, differentiable rendering, novel-view synthesis
- d. Simulation – physics-based virtual worlds, domain randomization, sim-to-real data generation

[10] *Computer Graphics: Principles and Practice, 3rd ed.* – John F. Hughes et al., Addison-Wesley (2013)

[11] *Fundamentals of Computer Graphics, 4th ed.* – Steve Marschner & Peter Shirley (eds.), CRC Press (2016)

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## Sub-area #3: Natural Language Processing

1. **Basic Concepts:** Statistical NLP vs. linguistics; Syntax vs. semantics; Formal language theory; Statistical language modeling
2. **Formal Language Theory and Chomsky Hierarchy:** DFA & reduction; NFA; Regular expressions; Context-free grammar; Context-dependent grammar; Turing machines, P vs. NP
3. **Statistical Models:** Probabilistic grammars; Parsing; Earley Parser; Hidden Markov Models; Conditional Random Fields
4. **Linear Language Modeling and Learned Embeddings:** One-hot and N-gram features; Word2Vec; Arithmetic on learned embeddings
5. **Neural Language Models and Recurrent Networks:** Neural language models, teacher forcing; Likelihood, perplexity, entropy; Lossless compression; Vanilla RNN; Vanishing gradients and long-range dependencies; LSTM; GRU; RWKV; Mamba
6. **Attention and Transformers:** Neural attention to machine translation; BERT; T5 model; GPT model; Multi-token prediction; Belief States; Diffusion language models
7. **Scaling Laws and New Topics:** Instruction fine-tuning; RL from Human Feedback; Kaplan scaling law, chinchilla; Synthetic data, Phi models; Reasoning tokens, DeepSeek-R1; AI Agent systems; Long context modeling; Retrieval augmented generation

### Reference Book

[1] *Introduction to Automata Theory, Languages, and Computation* – John Hopcroft

Jason Eisner NLP course: <https://www.cs.jhu.edu/~jason/465/>

[2] *Foundations of Statistical NLP* – Chris Manning

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## Sub-area #4: Reinforcement Learning

1. **Basic Concepts:** Markov Decision Process, value function, Bellman equation, exploration-exploitation trade-off; online vs. offline; model-free vs. model-based; planning vs. reactive policy; bandits vs. stateful RL; partial observability
2. **Offline-RL:** Behavior Cloning; Q-Learning; Deep Q-Learning
3. **Online-RL and Policy Gradient:** TRPO; PPO; GRPO; Actor-critic
4. **Model-Based Methods and Planning:** World Models; Dreamer; AlphaGo; MuZero
5. **Exploration:** Epsilon-greedy; Count-based; Elliptical Bonuses; Random Network Distillation; BYOL-Explore; MaxEnt RL; GFlowNet
6. **RL for LLMs:** RLHF; DPO; RL for reasoning

## Reference Book

- [1] [RL book] *Reinforcement Learning: Theory and Algorithms*. <https://rltheorybook.github.io/>
- [2] [RL Lectures] *Advanced Topics 2015*, David Silver.  
<https://davidstarsilver.wordpress.com/teaching/>
- [3] [RL Book] *Algorithms of Reinforcement Learning*, Csaba Szepesvari.  
<https://sites.ualberta.ca/~szepesva/rlbook.html>
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## Sub-area #5: Generative AI

### 1. Theoretical Foundations

- a. Transformer Architecture; Self-Attention; Mixture-of-Experts
- b. Diffusion Model
- c. Scaling Laws

### 2. Large Language Models (LLMs)

- a. Pre-training; Post-training; Alignment
- b. Long-Context Training
- c. Retrieval-Augment Generation
- d. Parameter-Efficient Fine-Tuning
- e. Safety, Red-Teaming, Guardrails
- f. Agent; Multi-Agent Systems

### 3. Vision and Language

- a. Contrastive Learning
- b. Multimodal Alignment
- c. Visual Instruction Tuning
- d. Masked/Generative Pretraining

## Reference Book

- [1] Vaswani, Ashish, et al. "Attention is all you need." *NIPS 30* (2017).
- [2] Kaplan, Jared, et al. "Scaling laws for neural language models." *arXiv:2001.08361* (2020).
- [3] Guo, Daya, et al. "Deepseek-r1: Incentivizing reasoning capability in LLMs via reinforcement learning." *arXiv:2501.12948* (2025).
- [4] Yang, An, et al. "Qwen3 technical report." *arXiv:2505.09388* (2025).
- [5] Liu, Haotian, et al. "Visual instruction tuning." *NeurIPS 36* (2023): 34892-34916.
- [6] Ho, J., Jain, A., & Abbeel, P. "Denoising diffusion probabilistic models." *NeurIPS 33* (2020): 6840-6851.

[7] <https://huggingface.co/learn/diffusion-course/en/unit0/1>

[8] <https://huggingface.co/learn/computer-vision-course/en/unit4/multimodal-models/vlm-intro>

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## Sub-area #6: Physical AI

### 1. Foundations & Modeling

- a. Robot Perception & 3D Vision
- b. Multi-view geometry basics ([3DV Book] Ch.1-3)
- c. Point cloud processing ([Robotics Book] Thrun Ch.6, Barfoot Ch.8)
- d. Robotic Dynamics
- e. Rigid-body kinematics/dynamics ([Robotics Book] Siciliano Ch.2-3)
- f. Force/impedance control ([Robotics Book] Siciliano Ch.8-9)

### 2. Algorithms & Planning

- a. Motion planning & Trajectory planning ([Robotics Book] Siciliano Ch.4 & 12)
- b. Optimal control & MPC ([Robotics Book] Siciliano Ch.8-9)
- c. Reinforcement Learning & Imitation Learning

### 3. Systems & Applications (30 %)

- a. Autonomous Mobile Robots
- b. Robot Localization ([Robotics Book] Siegwart Ch.5)
- c. Navigation & obstacle avoidance ([Robotics Book] Siegwart Ch.6)
- d. Physical AI Toolchains
- e. ROS/Gazebo simulation
- f. NVIDIA Isaac Sim/Omniverse

### Reference Book

[1] [3DV Book] Ma, Y. et al. *An Invitation to 3-D Vision* (2004).

[2] [Robotics Book] Siegwart, R. et al. *Introduction to Autonomous Mobile Robots* (2nd ed., 2011).

[3] [Robotics Book] Siciliano, B. et al. *Robotics: Modelling, Planning and Control* (3rd ed., 2010).

[4] [Robotics Book] Barfoot, T.D. *State Estimation for Robotics* (2022).

[5] [Robotics Book] Thrun, S. et al. *Probabilistic Robotics* (2005).

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## Sub-area #7: AI + Science

## 1. Inverse Problem

- a. Ill-posedness analysis
- b. Dimensionality reduction
- c. Regularization methods
- d. Prior modeling

## 2. Physics-Informed Learning

- a. Unfolding neural network
- b. Physics-informed neural networks
- c. Regularization flow
- d. Physics-constrained generative models
- e. Belief network
- f. Equivariant neural network
- g. Neural ordinary differential equation

## 3. Scientific Computing

- a. Scientific data and visualization
- b. Numerical analysis and simulation
- c. High performance computing
- d. Uncertainty quantification and optimal experimental design
- e. Probabilistic and causal inference
- f. Symbolic regression

### Reference Book:

[1] *Artificial Intelligence For Science: A Deep Learning Revolution*. Alok Choudhary, Geoffrey C Fox, Tony Hey.

[2] *Artificial Intelligence for Science (AI4S) Frontiers and Perspectives Based on Parallel Intelligence*. Qinghai Miao and Fei-Yue Wang. <https://link.springer.com/book/10.1007/978-3-031-67419-8>

[3] *Advanced Numerical Analysis: Machine Learning, Uncertainty Quantification, and Emerging Methods*. Machine L.

[4] *High-Performance Scientific Computing: Algorithms and Applications*. Michael W. Berry, Kyle A. Gallivan, et al.

[5] *Probabilistic Machine Learning: Advanced Topics (Adaptive Computation and Machine Learning series)*. Kevin P. Murphy.

[6] *Causality: Models, Reasoning and Inference*. Judea Pearl.

[7] *Pattern Recognition and Machine Learning*. Christopher M. Bishop.

<https://www.microsoft.com/en-us/research/wp-content/uploads/2006/01/Bishop-Pattern-Recognition-and-Machine-Learning-2006.pdf>

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## Sub-area #8: AI System

### 1. Architecture and Organization

#### 1) Digital Logic

- a. Logic expressions and Boolean functions
- b. Can use De Morgan's Law to simplify combination logic
- c. Sequential logic elements (flip-flops, latch)
- d. Basic timing constraints of sequential logic (synchronous circuits)
- e. Carry-ripple adder and array multiplier
- f. Signed and unsigned arithmetic
- g. Range, precision, and errors in floating-point arithmetic

#### 2) Computer Architecture

- a. Introduction to instruction set architecture, microarchitecture and system architecture
- b. Processor architecture – instruction types, register sets, addressing modes
- c. Memory hierarchy, latency and throughput
- d. Cache memories principles, replacement policies, and cache coherency
- e. Can use Amdahl's law to prioritize design decisions
- f. GPU architecture and programming model
- g. NPU architecture and programming model

### 2. Hardware-Software Codesign

#### 1) Quantization

- a. Number representations for lightweight NN (BF16, FP8, INT4)
- b. Can calculate the scale and bias value in a quantized NN layer
- c. Concept of post-training quantization and quantization-aware training

#### 2) Pruning

- a. Understand structured and unstructured sparsity
- b. Sparse encoding formats (bitmask, run-length encoding, compressed sparse row)

- c. Regularizations to construct sparsity in NN

### 3. Networking and Interconnect

- a. Background and history of networking and the Internet
- b. Network architectures
- c. Networks and protocols
- d. Distributed computing

#### Reference Book:

[1][Digital circuit book] *CMOS VLSI Design: A Circuits and Systems Perspective (4th Edition)*, Neil H. E. Weste, David Money Harris

[2][Arch book] *Computer Architecture: A Quantitative Approach (7th Edition)*, John L. Hennessy, David A. Patterson, Christos Kozyrakis

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**College of AI Graduate Program Committee – June 2025**